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JEE MAIN-2021

COMPUTER BASED TEST (CBT)

DATE : 26-02-2021 (EVENING SHIFT) | TIME : (3.00 pm to 6.00 pm)

Duration 3 Hours | Max. Marks: 300

QUESTION & SOLUTIONS

PART A : PHYSICS

Single Choice Type

This section contains 20 Single choice questions. Each question has 4 choices (1), (2), (3) and (4) for its answer, out of which Only One is correct. 1. If 'C' and 'V' represent capacity and voltage respectively then what are the dimensions of λ , where $\frac{C}{V}$? (1) $[M^{-2}L^{-3}l^{2}T^{6}]$ (2) $[M^{-3}L^{-4}l^{3}T^{7}]$ (3) $[M^{-1}L^{-3}l^{-2}T^{-7}]$ (4) $[M^{-2}L^{-4}l^{3}T^{7}]$ Ans. (4) $\frac{C}{V} = \frac{Q/V}{V} = \frac{Q}{V^2}$ Sol. $V = \frac{\text{work}}{Q}$ $\frac{Q^3}{(work)^2} \quad \frac{(It)^3}{(F.s)^2}$ $\frac{[I^{3}T^{3}]}{[ML^{2}T^{2}]} \quad [M^{2}L^{4}I^{3}T^{7}]$ The length of metallic wire is ℓ_1 when tension in it is T_1 . It is ℓ_2 when the tension is T_2 . The original length 2. of the wire will be : (4) $\frac{T_1\ell_1 - T_2\ell_2}{T_2 - T_1}$ (1) $\frac{\ell_1 - \ell_2}{2}$ (2) $\frac{T_2 \ell_1 \quad T_1 \ell_2}{T_1 \quad T_2}$ 1-JEE Ans. (3) Assuming Hooke's law to be valid. Sol. $T \propto (\Delta \ell)$ $T = k(\Delta \ell)$ Let, ℓ_0 = natural length (original length) So, $T_1 = k(\ell_1 - \ell_0)$ & $T_2 = k(\ell_2 - \ell_0)$ $\frac{\mathsf{T}_1}{\mathsf{T}_2} \quad \frac{\ell_1 \quad \ell_0}{\ell_2 \quad \ell_0}$ $\ell_0 = \frac{T_2\ell_1 - T_1\ell_2}{T_2 - T_1}$ 3. An aeroplane, with its wings spread 10 m, is flying at a speed of 180 km/h in a horizontal direction. The total intensity of earth's field at that part is 2.5×10^{-4} Wb/m² and the angle of dip is 60°. The emf induced

between the tips of the plane wings will be :

(1) 108.25 mV (2) 54.125 mV (3) 88.37 mV (4) 62.50 mV

Ans.	(1)			
Sol.	[BVL] BVL sin			
	(2.5 10 ^₄ T) 180	$\frac{5}{18}$ m/s (10m) sin60°		
	= 108.25 × 10 ⁻³ V			
4.	A tuning fork A of unki	nown frequency produc	es 5 beats/s with a fork	of known frequency 340 Hz. When
		t frequency decreases		
	(1) 342 Hz	(2) 345 Hz	(3) 335 Hz	(4) 338 Hz
Ans.	(3)			
Sol.	Initially beat frequency	-		
	so, $\rho_A = 340 \pm 5 = 345$			
	after filing frequency in	0.1		
	so, new value of frequ			
	Now, beat frequency = \Rightarrow new $\rho_A = 340 \pm 2 =$			
-		ncy of A is $\rho_A = 335$ Hz		
5.		H.M., the graph of velo		
			(2) An ollingo	\sim (4) A boliv
Δns	(1) A circle	(2) A parabola	(3) An ellipse	(4) A helix
Ans.	(3)	(2) A parabola	(3) An ellipse	(4) A helix
Ans. Sol.	(3) $v^2 = \omega^2 (A^2 - x^2)$	(2) A parabola	(3) An ellipse	(4) A helix
	(3)	(2) A parabola	(3) An ellipse	(4) A helix
	(3) $v^{2} = \omega^{2}(A^{2} - x^{2})$ $\frac{v^{2}}{2} x^{2} A^{2}$ $\frac{v^{2}}{(A^{2})^{2}} \frac{x^{2}}{A^{2}} 1$		(3) An ellipse	(4) A helix
	(3) $v^{2} = \omega^{2}(A^{2} - x^{2})$ $\frac{v^{2}}{2} x^{2} A^{2}$ $\frac{v^{2}}{(A^{2})^{2}} \frac{x^{2}}{A^{2}} 1$		(3) An ellipse	(4) A helix
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Sol.	(3) $v^{2} = \omega^{2}(A^{2} - x^{2})$ $\frac{v^{2}}{2} x^{2} A^{2}$ $\frac{v^{2}}{(A)^{2}} \frac{x^{2}}{A^{2}} 1$ This is an equation of The trajectory of a pro- are respectively the h angle of projection q a	an ellipse. Djectile in a vertical plar orizontal and vertical d	t attained H are respected	re α and β are constants and x & y le from the point of projection. The stively given by :
Sol.	(3) $v^{2} = \omega^{2}(A^{2} - x^{2})$ $\frac{v^{2}}{2} x^{2} A^{2}$ $\frac{v^{2}}{(A)^{2}} \frac{x^{2}}{A^{2}} 1$ This is an equation of The trajectory of a pro- are respectively the h angle of projection q a	an ellipse. Djectile in a vertical plan orizontal and vertical d	t attained H are respected	re α and β are constants and x & y le from the point of projection. The stively given by :
Sol.	(3) $v^{2} = \omega^{2}(A^{2} - x^{2})$ $\frac{v^{2}}{2} x^{2} A^{2}$ $\frac{v^{2}}{(A)^{2}} \frac{x^{2}}{A^{2}} 1$ This is an equation of The trajectory of a pro- are respectively the h angle of projection q a	an ellipse. Djectile in a vertical plar orizontal and vertical d	t attained H are respected	re α and β are constants and x & y le from the point of projection. The stively given by :
Sol. 6.	(3) $v^{2} = \omega^{2}(A^{2} - x^{2})$ $\frac{v^{2}}{2} x^{2} A^{2}$ $\frac{v^{2}}{(A)^{2}} \frac{x^{2}}{A^{2}} 1$ This is an equation of The trajectory of a pro- are respectively the h- angle of projection q a (1) tan ¹ , $\frac{2}{4}$	an ellipse. Djectile in a vertical plar orizontal and vertical d	t attained H are respected	re α and β are constants and x & y le from the point of projection. The stively given by :
Sol. 6. Ans.	(3) $v^{2} = \omega^{2}(A^{2} - x^{2})$ $\frac{v^{2}}{2} x^{2} A^{2}$ $\frac{v^{2}}{(A)^{2}} \frac{x^{2}}{A^{2}} 1$ This is an equation of The trajectory of a pro- are respectively the h- angle of projection q a (1) tan ¹ , $\frac{2}{4}$ (1)	an ellipse. bjectile in a vertical plan orizontal and vertical d and the maximum heigh (2) $\tan^{-1}, \frac{2}{2}$	t attained H are respected	re α and β are constants and x & y le from the point of projection. The stively given by :

Tan
$$\theta$$
 = $\alpha \Rightarrow \theta$ = tan⁻¹ α

$$\frac{1}{2} \frac{g}{u^2 \cos^2}$$

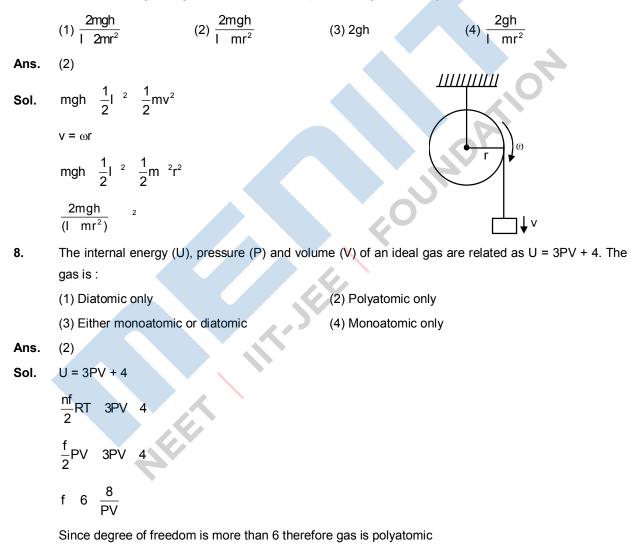
$$u^2 \quad \frac{g}{2 \cos^2}$$
Maximum height : H
$$H \quad \frac{u^2 \sin^2}{2\pi} \quad \frac{g}{2 \cos^2}$$

H
$$\frac{u^2 \sin^2}{2g}$$
 $\frac{g}{2 \cos^2} \frac{\sin^2}{2g}$
H $\frac{\tan^2}{4}$ $\frac{2}{4}$

7.

ŀ

A cord is wound round the circumference of wheel of radius r. The axis of the wheel is horizontal and the moment of inertia about it is I. A weight mg is attached to the cord at the end. The weight falls from rest. After falling through a distance 'h', the square of angular velocity of wheel will be :



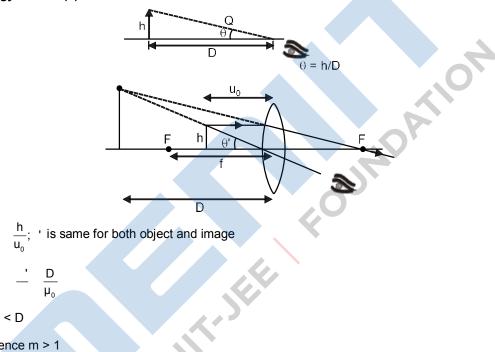
9. Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R. Assertion A : For a simple microscope, the angular size of the object equals the angular size of the image.

Reason R : Magnification is achieved as the small object can be kept much closer to the eye than 25 cm and hence it subtends a large angle. In the light of the above statements, choose the most appropriate answer from the options given below :

- (1) A is true but R is false
- (2) Both A and R are true but R is NOT the correct explanation of A.
- (3) Both A and R are true and R is the correct explanation of A
- (4) A is false but R is true
- Ans. (3)

Sol.

Zigyan Ans. (2)



$$m - \frac{D}{\mu_0}$$

 $u_0 < D$

Hence m > 1

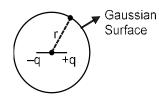
10. Given below are two statements :

> Statement I: An electric dipole is placed at the centre of a hollow sphere. The flux of electric field through the sphere is zero but the electric field is not zero anywhere in the sphere.

> Statement II: If R is the radius of a solid metallic sphere and Q be the total charge on it. The electric field at any point on the spherical surface of radius r (< R) is zero but the electric flux passing through this closed spherical surface of radius r is not zero. In the light of the above statements, choose the correct answer from the options given below :

- (1) Both Statement I and Statement II are true
- (2) Statement I is true but Statement II is false
- (3) Both Statement I and Statement II are false
- (4) Statement I is false but Statement II is true.

Ans. (2)



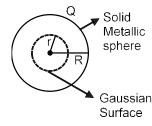
Sol.

 $\bigcirc \vec{E} \vec{ds} \frac{q_{in}}{0} 0$

Flux of \vec{E} through sphere is zero.

But $\bigcirc \vec{E} \ \vec{ds} \ 0 \ \vec{E} \ \vec{ds} \ 0$ for small section ds only

Statement-2



As change encloses within gaussian surface is equal to zero.

 $\overrightarrow{\mathsf{DE}} \, \overrightarrow{\mathsf{ds}} \, 0$

Option (2) statement-1 correct statement-2 false.

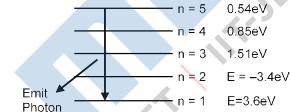
11. The recoil speed of a hydrogen atom after it emits a photon in going from n = 5 state to n = 1 state will be :

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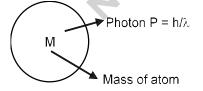
(1) 4.17 m/s	(2) 2.19 m/s	(3) 3.25 m/s	(4) 4.34 m/s
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Ans. (1)

Sol.



(ΔE) Releases when photon going from n = 5 to n = ΔE = (13.6 – 0.54) eV = 13.06 eV



 $P_i = P_f$ (By linear momentum conservation)

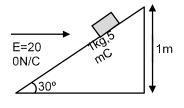
 $0 \quad \frac{h}{M} \quad Mv \quad V_{\text{Recoil}} \quad \frac{h}{M} \qquad \qquad \dots (i)$

8 E
$$\frac{hc}{M}$$
 M mcV_{Recoll}
 $V_{\text{Recosl}} = \frac{E}{Mc} \frac{13.06}{1.67} \frac{10}{10^{27}} \frac{10^{19}}{3} \frac{4.17 \text{ m/sec}}{1.10^{10} \text{ JU}}$
12. Find the peak current and resonant frequency of the following circuit (as shown in figure).
 $\int \frac{100 \text{ mH}}{100 \text{ mH}} \frac{100 \text{ µF}}{100 \text{ µF}}$
(1) 0.2 A and 50 Hz (2) 0.2 A and 100 Hz (3) 2 A and 100 Hz (4) 2A and 50 Hz
Ans. (1)
Sol. As given z $\sqrt{(X_1 - X_2)^2 - R^2}$
 $X_1 = \omega_1 = 100 \times 100 \times 10^{-3} = 10\Omega$
 $X_c = \frac{1}{c} - \frac{1}{100} \frac{1}{100} \frac{10^{-9}}{10^{9}} \frac{100}{12^2}$
 $= 30 \times 5 = 150\Omega$
 $I_{\text{Lown}} = \frac{X}{Z} - \frac{30}{150} - \frac{1}{5} \text{ amp} - 0.2 \text{ amp}$
& for resonant frequency
 $L = \frac{1}{L} = \frac{2}{LC} - \frac{1}{\sqrt{LC}}$
8 f $\frac{1}{2\sqrt{LC}} = \frac{1}{2\sqrt{100}} \frac{1}{10^{-3}} \frac{1}{10^{9}} \frac{1}{10^{-9}} \frac{1}{10^{-9}} \frac{1}{10^{-9}} \frac{1}{10^{-9}}$
13. An inclined plane making an angle of 30° with the horizontal is placed in a uniform horizontal electric

13.

field $200\frac{N}{C}$ as shown in the figure. A body of mass 1kg and charge 5 mC

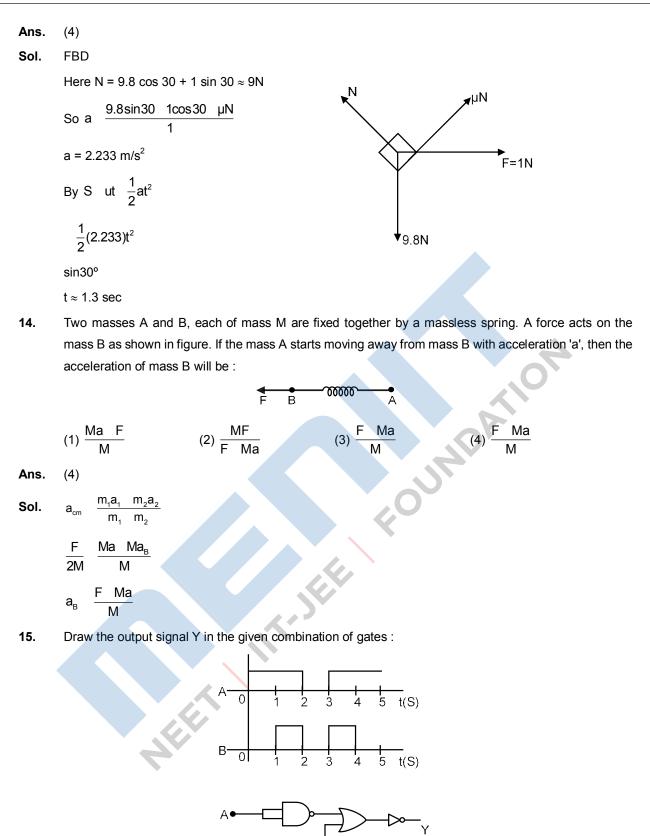
is allowed to slide down from rest at a height of 1m. If the coefficient of friction is 0.2, find the time taken by the body to reach the bottom. [g =



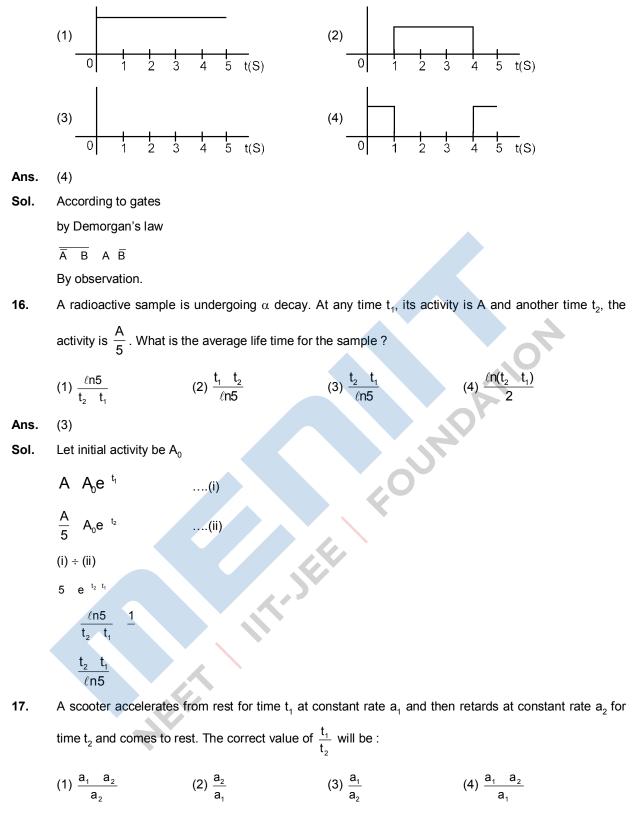
9.8 m/s², sin 30°
$$\frac{1}{2}$$
; cos 30° $\frac{\sqrt{3}}{2}$]
(1) 0.92 s (2) 0.46 s

(4) 1.3 s

(3) 2.3 s



B



Ans. (2)

Sol. Draw vt curve

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	$\tan_1 a_1 \frac{V_{max}}{t}$
	v_{max}
	& tan $_2$ a_2 $\frac{v_{max}}{t_2}$
	÷ above $\theta_1 \qquad \theta_2$
	$\frac{\mathbf{t}_1}{\mathbf{t}_2} \frac{\mathbf{a}_2}{\mathbf{a}_1}$
18.	Given below are two statements :
	Statement I: A second's pendulum has a time period of 1 second.
	Statement II : It takes precisely one second to move between the two extreme positions.
	In the light of the above statements, choose the correct answer from the options given below :
	(1) Both Statement I and Statement II are false. (2) Statement I is false but Statement II is true
	(3) Statement I is true but Statement II is false (4) Both Statement I and Statement II are true.
Ans.	(2)
Sol.	Second pendulum has a time period of 2 sec so statement 1 is false but from one extreme to other it takes only half the time period so statement 2 is true.
19.	A wire of 1Ω has a length of 1m. It is stitched till its length increases by 25%. The percentage change in
	resistance to the nearest integer is :-
	(1) 56% (2) 25% (3) 12.5% (4) 76%
Ans.	(1)
Sol.	$R_0 = 1\Omega$ $R_1 = ?$
	$\ell_0 = 1m$ $\ell_1 = 1.25m$
	$A_0 = A$
	As volume of wire remains constant so
	$A_0 \ell_0 A_1 \ell_1 A_1 \frac{\ell_0 A_0}{\ell_1}$
	Now
	Resistance (R) $\frac{\ell}{A}$
	$\frac{R_{0}}{R_{1}} = \frac{\ell_{1}/A_{0}}{\ell_{1}/A_{1}}$
	$\frac{1}{R_{1}} \frac{\ell_{0}}{A_{0}} \frac{\ell_{0}A_{0}}{\ell_{1} \ell_{1}} \qquad \qquad R_{1} \frac{\ell_{1}^{2}}{\ell_{0}^{2}} 1.5625$
	So % change in resistance
	$\frac{R_1 - R_0}{R_0}$ 100%

	$\frac{1.5625 \ 1}{1}$ 100%
	= 56.25%
20.	The incident ray, reflected ray and the outward drawn normal are denoted by the unit vectors \ddot{a} \ddot{b} and \ddot{c}
	respectively. Then choose the correct relation for these vectors.
	(1) \vec{b} \vec{a} $2\vec{c}$ (2) \vec{b} $2\vec{a}$ \vec{c} (3) \vec{b} \vec{a} $2\vec{a}$ \vec{c} \vec{c} (4) \vec{b} \vec{a} \vec{c}
Ans.	(3)
Sol.	ā sin î cos ĵ
	\vec{b} sin \hat{i} cos \hat{j}
	c ĵ → l
	ā 2 ā c c sin î cos ĵ

Numeric Value Type

This Section contains 10 Numeric Value Type question, out of 10 only 5 have to be done.

1. The volume V of a given mass of monoatomic gas changes with temperature T according to the relation V = $KT^{2/3}$. The workdone when temperature changes by 90 K will be xR. The value of x is [R = universal gas constant]

...

Sol. We know that work done is

w PdV ... (1)
P
$$\frac{nRT}{V}$$
 ... (2)

 $\frac{nRT}{V} dv$ W ... (3) and V = $KT^{2/3}$

... (4) $\frac{nRT}{KT^{2/3}} dv$ W ... (5)

$$\Rightarrow$$
 from (4) : dv $\frac{2}{3}$ KT ^{1/3}dT

W
$$\int_{T_1}^{T_2} \frac{nRT}{KT^{2/3}} \frac{2}{3} K \frac{1}{T^{1/3}} dT$$

W $\frac{2}{3}$ nR T₂ T₁ ... (6) \Rightarrow T₂ – T₁ = 90 K ... (7)

W $\frac{2}{3}$ nR 90

Assuming 1 mole of gas

So W = 60R

2. If the highest frequency modulating a carrier is 5 kHz, then the number of AM broadcast stations accommodated in a 90 kHz bandwidth are

⇒ W = 60 nR

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Ans. (9)

Sol. B. W. (Bandwidth) = 2 × maximum frequency at modulating signal

```
= 2 × 5 kHz
```

= 10 kHz

- ... No of stations accommodate
 - 90 10

3. Two stream of photons, possessing energies equal to twice and ten times the work function of metal are incident on the metal surface successively. The value of ratio of maximum velocities of the photoelectrons emitted in the two respective cases is x : y. The value of x is

Ans. (1)

Sol. $KE_{max} = hv - \phi$

$$\frac{1}{2}mv^{2} h$$

$$v \sqrt{\frac{2(h)}{m}}$$

Given $hv_1 = 2\phi$

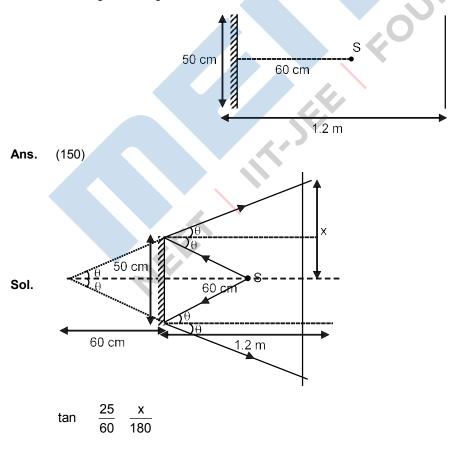
1 3

 $hv_2 = 10 \phi$

$$\frac{v_1}{v_2} \sqrt{\frac{h_1}{h_2}}$$

$$\frac{v_1}{v_2} \sqrt{\frac{2}{10}}$$

4. A point source of light S, placed at a distance 60 cm infront of the centre of a plane mirror of width 50 cm, hangs vertically on a wall. A man walks infront of the mirror along a line parallel to the mirror at a distance 1.2 m from it (see in the figure). The distance between the extreme points where he can see the image of the light source in the mirror is cm.



x = 75 cm

so distance between extreme point = $2x = 2 \times 75 = 150$ cm

5. A particle executes S.H.M. with amplitude 'a' and time period V. The displacement of the particle when its speed is half of maximum speed is $\frac{\sqrt{xa}}{2}$. The value of x is

Sol. $V_{max} = A\omega$ $\sqrt{A^2 x^2}$

$$\frac{A}{2} \sqrt{A^2 x^2}$$

$$\frac{A^2}{4} A^2 x^2$$

$$x^2 \frac{3A^2}{4}$$

$$x \frac{\sqrt{3}}{2}A$$

6. 27 similar drops of mercury are maintained at 10 V each. All these spherical drops combine into a single big drop. The potential energy of the bigger drop is times that of a smaller drop.

(27) $\frac{4}{3}$ r³ $\frac{4}{3}$ R³ Sol.

R = 3r

FOUR Potential energy of smaller drop :

$$U_1 = \frac{3}{5} \frac{kq^2}{r}$$

Potential energy of bigger drop :

$$U = \frac{3}{5} \frac{kQ^{2}}{R}$$

$$U = \frac{3}{5} \frac{k}{R} \frac{27q^{2}}{R}$$

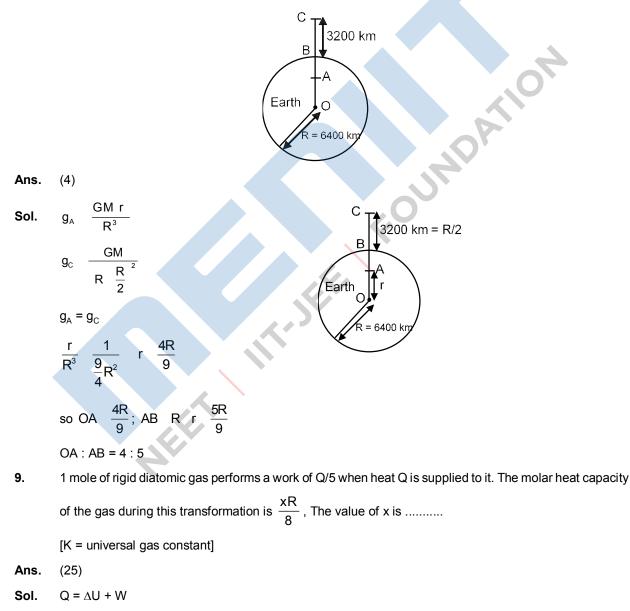
$$U = \frac{3}{5} \frac{k}{3} \frac{27}{3r} \frac{27}{3r}$$

$$U = \frac{27}{3} \frac{27}{3} \frac{3}{5} \frac{kq}{r}$$

7. Time period of a simple pendulum is T. The time taken to complete 5/8 oscillations starting from mean position is — T. The value of a is

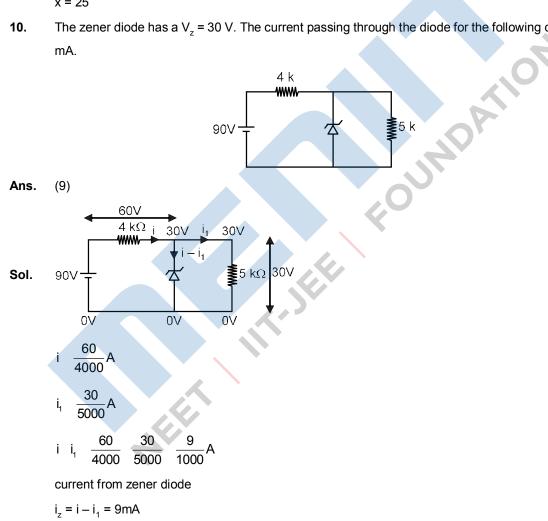
Ans. (7) Sol. $\frac{5}{8}$ th of oscillation $\frac{1}{2} \cdot \frac{1}{8}^{th}$ of oscillation $\pi + \theta = \omega t$ $\overline{6} \quad \frac{2}{T} \cdot t$ $\frac{7}{6} \quad \frac{2}{T} \cdot t$ $t \quad \frac{7T}{12}$

8. In the reported figure of earth, the value of acceleration due to gravity is same at point A and C but it is smaller than that of its value at point B (surface of the earth). The value of OA : AB will be x : y. The value of x is



 $U \frac{Q}{5}$ Q $U \frac{4Q}{5}$ $nC_v T = \frac{4}{5}nC T$ $\frac{5}{4}C_v$ C C $\frac{5}{4} \frac{f}{2} R \frac{5}{4} \frac{5}{2} R$ $C \frac{25}{8}R$ x = 25

The zener diode has a V_z = 30 V. The current passing through the diode for the following circuit is 10. mA.



PART B : CHEMISTRY

Single Choice Type

This section contains **20 Single choice questions**. Each question has 4 choices (1), (2), (3) and (4) for its answer, out of which **Only One** is correct.

1. Which of the following forms of hydrogen emits low energy β^- particles?

```
(1) Deuterium _{1}^{2}H (2) Tritium _{1}^{3}H
```

(3) Protium ¹H

(4) Proton H⁺

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Ans. (2)
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Sol. For tritium $\binom{3}{1}$ H)

No. of neutron (n) = 2No. of proton (p) = 1

 $\frac{n}{p}$ 2

 $\therefore \frac{n}{n}$ is high,

tritium will emit β particle.

2. Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R

Assertion A : In $T\ell I_3$, isomorphous to CsI_3 , the metal is present in +1 oxidation state.

Reason R : $T\ell$ metal has fourteen f electrons in the electronic configuration.

In the light of the above statements, choose the most appropriate answer from the options given below:

- (1) A is correct but R is not correct
- (2) Both A and R are correct and R is the correct explanation of A.
- (3) A is not correct but R is correct
- (4) Both A and R are correct but R is NOT the correct explanation of A.

Ans. (4)

Sol. $T\ell I_3 = T\ell \& I_3$

 CsI_3 Cs & I_3

[Both have same crystalline structure is called isomorphous]

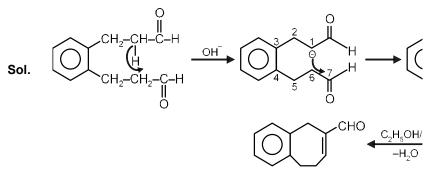
 $T\ell_{81} = Xe_{54} + 4f^{14}$, $5d^{10}$, $6s^2$

(It is correct due to present 14 f electrons in $T\ell^{\oplus}$ ion)

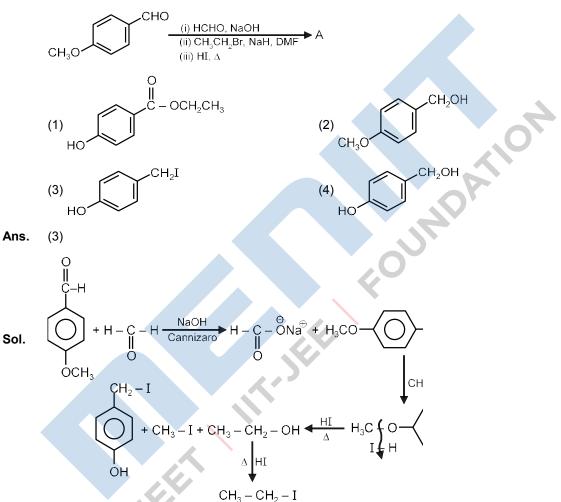
3. Match List-I with List-II List-I List-II (a) Sucrose (i) β -D-Galactose and β -D-Glucose (b) Lactose (ii) α -D-Glucose and β -D-Fructose α -D-Glucose and α -D-Glucose (C) Maltose (iii) Choose the correct answer from the options given below : **Options**: (1) (a) \rightarrow (i), (b) \rightarrow (iii), (c) \rightarrow (ii) (2) (a) \rightarrow (iii), (b) \rightarrow (i), (c) \rightarrow (iii) (3) (a) \rightarrow (ii), (b) \rightarrow (i), (c) \rightarrow (iii) (4) (a) \rightarrow (iii), (b) \rightarrow (ii), (c) \rightarrow (i) Ans. (3) Sol. (1) Sucrose $\rightarrow \alpha$ -D-Glucose and β -D-Fructose (2) Lactose $\rightarrow \beta$ -D-Galactose and β -D-Glucose (3) Maltose $\rightarrow \alpha$ -D-Glucose and α -D-Glucose UNDATIC $a \rightarrow II$ $b \rightarrow I$ $c \rightarrow III$ 4. A. Phenyl methanamine B. N,N-Dimethylaniline C. N-Methyl aniline D. Benzenamine Choose the correct order of basic nature of the above amines. (2) D > C > B > A(3) D > B > C > A (1) A > C > B > D(4) A > B > C > DAns. (4) CH₃ . N –CH₃ NH_2 $CH_2 - NH_2$ NH -CH₃ Sol. (C) (B) (D)(A) B.S. order (A) > (B) > (C) > (D)5. The correct order of electron gain enthalpy is (1) S > Se > Te > O (2) Te > Se > S > O (3) O > S > Se > Te (4) S > O > Se > Te Ans. (1) Sol. correct order of electron gain enthalpy is :-O < S > Se > Te \Rightarrow S > Se > Te > O (Oxygen shows least electron gain enthalpy due to small size of atom)

6.	In $\overset{1}{C}H_2$ $\overset{2}{C}$ $\overset{3}{C}H$ $\overset{4}{C}H_3$ molecule, the hybridization of carbon 1,2,3 and 4 respectively are :			
	(1) sp ³ , sp, sp ³ , sp ³	(2) sp ² , sp ² , sp ² , sp ³	(3) sp^2 , sp , sp^2 , sp^3	(4) sp^2 , sp^3 , sp^2 , sp^3
Ans.	(3)			
Sol.	[CH ₂ C ³ CH CH ₃]	l .		
301.	- 2 0-			
	$\begin{bmatrix} H & H \\ Sp^2 & Sp & Sp^2 & Sp^3 \\ C & C & C & C & -C & -H \\ H & H & H & H \end{bmatrix}$	H		
7.	Seliwanoff test and Xa	anthoproteic test are used	for the identification of	and respectively
	(1) Aldoses, ketoses	(2) Proteins, ketoses	(3) Ketoses, proteins	(4) Ketoses, aldoses
Ans.	(3)			
Sol.	Seliwanoff test for ket	ose and Xenthoprotic tes	t for proteins.	
8.	2,4-DNP test can be u	ised to identify :		
Ans.	(1) Amine (2)	(2) Aldehyde	(3) Ether	(4) Halogens
Sol.		for the identification of ca	arbonyl compounds.	
9.				tion of functional groups present
	in and res	spectively.		
Ans.	(1) Alcohol, phenol (3)	(2) Amine, alcohol	(3) Alcohol, amine	(4) Amine, phenol
Sol. 10.	Ceric ammonium nitra Which pair of oxides is	te for alcohol and CHCl ₃ , s acidic in nature?	KOH is carbyl amine te	st for primary amines
	(1) B ₂ O ₃ , CaO	(2) B ₂ O ₃ , SiO ₂	(3) N₂O, BaO	(4) CaO, SiO ₂
Ans.	(2)			
Sol.	CaO, BaO Basic N B_2O_3 , SiO ₂ Acidic N_2O Neutral oxide			
11.	Identify A in the given	chemical reaction,		
	CH ₂ CH ₂ CHO CH ₂ CH ₂ CHO	$ \xrightarrow{\text{NaOH}}_{C_2H_5\text{OH},H_2\text{O}} A \text{ (Major} $	Product)	
	(1) CH	0	(2) CH ₂ CH ₂ CH ₂ CC	
	(3) (3)			

Ans. (3)



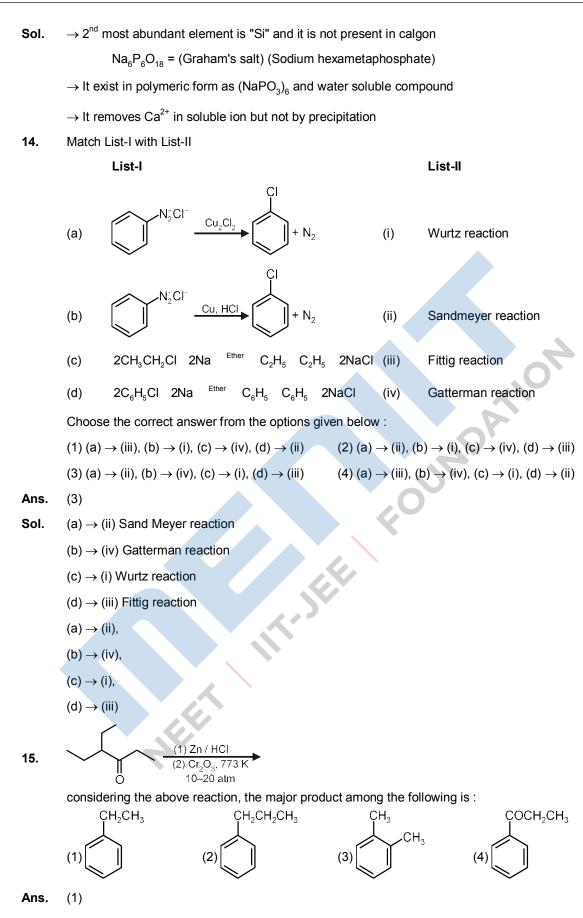
12. Identify A in the following chemical reaction

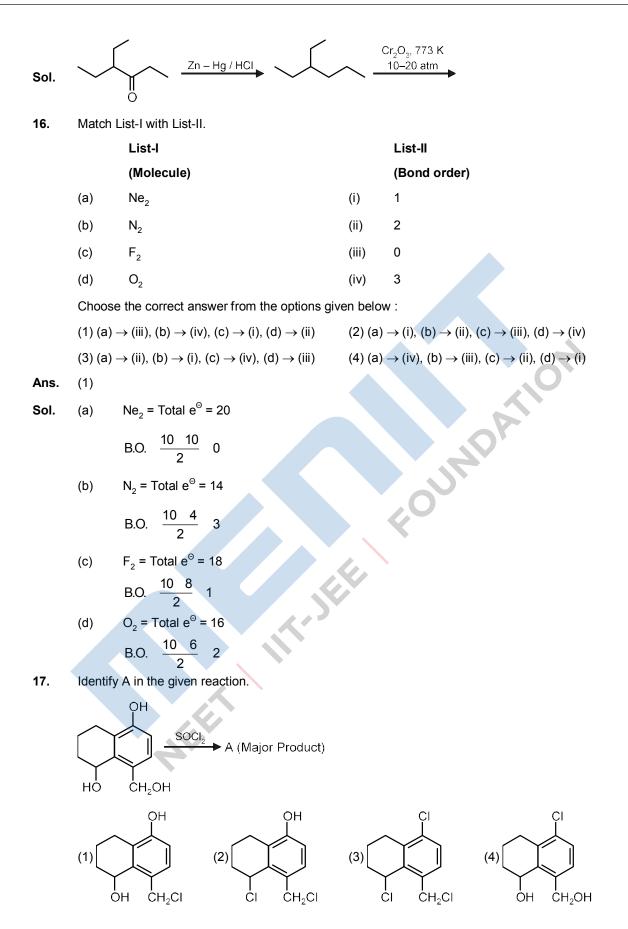


Calgon is used for water treatment. Which of the following statement is NOT true about Calgon?
 (1) Calgon contains the 2nd most abundant element by weight in the Earth's crust.

- (2) It is polymeric compound and is water soluble.
- (3) It is also known as Graham's salt
- (4) It does not remove Ca^{2+} ion by precipitation.

Ans. (1)





Ans. (2) OH OH SOCI Sol. ĠН ĊH₂OH ĊI CH₂Cl 18. Match List-I with List-II. List-I List-II Siderite Cu (a) (i) (b) Calamine (ii) Са (C) Malachite (iii) Fe (d) Cryolite (iv) AI Zn (v) Choose the correct answer from the options given below : (2) (a) \rightarrow (i), (b) \rightarrow (ii), (c) \rightarrow (v), (d) \rightarrow (iii) (1) (a) \rightarrow (iii), (b) \rightarrow (i), (c) \rightarrow (v), (d) \rightarrow (ii) (4) (a) \rightarrow (i), (b) \rightarrow (ii), (c) \rightarrow (iii), (d) \rightarrow (iv) (3) (a) \rightarrow (iii), (b) \rightarrow (v), (c) \rightarrow (i), (d) \rightarrow (iv) Ans. (3) OUNE Sol. (a) Siderite = $FeCO_3$ = Fe-metal (b) Calamine = ZnCO₃ = Zn-metal (c) Malachite = $Cu(OH)_2$. $CuCO_3$ = Cu-metal (d) Cryolite = Na_3AIF_6 = Al-metal 19. The nature of charge on resulting colloidal particles when FeCl₃ is added to excess of hot water is : (2) Sometimes positive and sometimes negative (1) Positive (3) Neutral (4) Negative Ans. (1) Sol. If FeCl₃ is added to hot water, a positively charged sol, hydrated ferric oxide is formed due to adsorption of Fe³⁺ ions. Fe₂O₃. xH₂O/Fe³⁺ Positively charged. 20. Match List-I with List-II. List-I List-II Sodium Carbonate (a) (i) Deacon (b) Titanium (ii) Castner-Kellner Van-Arkel (C) Chlorine (iii) (d) Sodium hydroxide (iv) Solvay Choose the correct answer from the options given below :

(2) (a) \rightarrow (i), (b) \rightarrow (iii), (c) \rightarrow (iv), (d) \rightarrow (ii)

(4) (a) \rightarrow (iii), (b) \rightarrow (ii), (c) \rightarrow (i), (d) \rightarrow (iv)

$$(1) (a) \rightarrow (iv), (b) \rightarrow (iii), (c) \rightarrow (i), (d) \rightarrow (ii)$$

$$(3) (a) \rightarrow (iv), (b) \rightarrow (i), (c) \rightarrow (ii), (d) \rightarrow (iii)$$

Ans. (1)

- Sol. (a) Sodium carbonate is prepared by Solvay process
 - (b) Titanium is refined by Van-Arkel process
 - (c) Chlorine is prepared by Deacon process
 - (d) Sodium hydroxide is prepared by Castner-Kellner process

FOUNDATIC JEE

Numeric Value Type

	This Section contains 10 Numeric Value Type question , out of 10 only 5 have to be done.		
1.	The NaNO ₃ weighed out to make 50 mL of an aqueous solution containing 70.0 mg Na ^{$+$} per mL is		
	g. (Rounded off to the nearest integer)		
	[Given : Atomic weight in g mol ⁻¹ – Na : 23 ; N : 14 ; O : 16]		
Ans.	(13)		
Sol.	Na [⁺] present in 50 ml		
	70mg 1ml 50ml 3500mg 3.5gm		
	moles of Na $\frac{3.5}{23}$ moles of NaNO ₃		
	weight of NaNO ₃ $\frac{3.5}{23}$ 85 12.993 gm		
2.	Emf of the following cell at 298 K in V is $x \times 10^{-2}$. Zn Zn ²⁺ (0.1 M) Ag ⁺ (0.01 M) Ag The value of x is (Rounded off to the nearest integer)		
	[Given : $E_{Zn^2/Zn}^0$ 0.76V ; $E_{Ag/Ag}^0$ 0.80V ; $\frac{2.303 \text{ RT}}{F}$ 0.059]		
Ans.	(147)		
Sol.	$Zn(s) \longrightarrow Zn^{2+}(aq.) + 2e^{-}$		
	$2Ag^{+}(aq.) + 2e^{-} \longrightarrow 2Ag(s)$		
	$Zn(s) + 2Ag^{+}(aq.) \longrightarrow 2Zn^{2+}(aq.) + 2Ag(s)$		
	$E_{cell}^0 = E_{Ag/Ag}^0 = E_{Zn^2/Zn}^0$		
	= 0.80 - (-0.76)		
	= 1.56 V		
	$E_{cell} = \frac{1.56 - \frac{0.059}{2} \log \frac{[Zn^2]}{[Ag]^2}}{[Ag]^2}$		
	$1.56 \frac{0.059}{2} \log \frac{0.1}{(0.01)^2}$		
	1.56 $\frac{0.059}{2}$ 3		
	= 1.56 - 0.0885		
	= 1.4715		
	$= 147.15 \times 10^{-2}$		

3. When 12.2 g of benzoic acid is dissolved in 100 g of water, the freezing point of solution was found to $be -0.93^{\circ}C (K_f (H_2O) = 1.86K \text{ kg mol}^{-1})$. The number (n) of benzoic acid molecules associated (assuming 100% association) is _____.

Ans. (2) $\Delta T_f = i \times k_f \times m$ Sol. 0.93 i 1.86 $\frac{12.2}{122 \ 100}$ 1000 0 i <u>0.93</u> 0.5 $i \ 1 \ \frac{1}{n} \ 1$ $\frac{1}{2}$ 1 $\frac{1}{n}$ 1 1 n = 2 4. The average S–F bond energy in kJ mol⁻¹ of SF₆ is _____.(Rounded off to the nearest integer) [Given : The values of standard enthalpy of formation of SF₆(g), S(g) and F(g) are -1100, 275 and 80 kJ mol⁻¹ respectively.] FOUND Ans. (309) Sol. $SF_{e}(g) \rightarrow S(g) + 6F(g)$ If \in - bond enthalpy $\Delta_{r}H = 6 \times \in_{S-F}$ 1-366 $= \Delta_{f} H(S,g) + 6 \times \Delta_{f} H(F,g) - \Delta_{f} H(SF_{6},g)$ = 275 + 6 × 80 - (-1100) = 1855 kJ s F $\frac{1855}{6}$ 309.16 kJ/mol. A ball weighing 10 g is moving with a velocity of 90 ms⁻¹. If the uncertainty in its velocity is 5%, then the 5. uncertainty in its position is $\times 10^{-33}$ m. (Rounded off to the nearest integer) [Given : $h = 6.63 \times 10^{-34} \text{ Js}$] Ans. (1)5 100 90 Sol.

= 4.5 m/s

$$v x \frac{g}{4 m}$$

- $x \frac{h}{4 m}$ 6.63 10³⁴ 4 3.14 0.01 4.5 $= 1.17 \times 10^{-33}$ 6. The number of octahedral voids per lattice site in a lattice is _____.(Rounded off to the nearest integer) Ans. (1) Sol. If number of lattice points are N. then effective octahedral voids = N So, octahedral voids / lattice site = 1 7. In mildly alkaline medium, thiosulphate ion is oxidized by MnO₄ to "A". The oxidation state of sulphur in "A" is Ans. (6) MnO_4 $S_2O_3^2$ MnO_2 SO_4^2 Sol. Oxidation state of 'S' in SO²₄ = + 6 The number of stereoisomers possible for [Co(ox)₂(Br)(NH₃)]²⁻ is 8. [ox = oxalate] Ans. (3) Total number of stereoisomers in $[Co(ox)_2Br(NH_3)]^{2\Theta}$ i.e. $\approx [M(AA)_2ab]^{2-1}$ Sol. b (b (cis) (trans) Ò (d)
 - \rightarrow cis is optically active isomers and trans is optically inactive isomer
 - \rightarrow Hence total isomers is = 3
- 9. If the activation energy of a reaction is 80.9 kJ mol⁻¹, the fraction of molecules at 700 K, having enough energy to react to form products is e^{-x} . The value of x is _____. (Rounded off to the nearest integer) [Use R = 8.31 J K⁻¹ mol⁻¹]

Sol. Fraction of molecules to have enough energy to react = $e^{-Ea/RT}$

So, X
$$\frac{E_a}{RT}$$

$$\frac{80.9 \quad 10^3}{8.31 \quad 700}$$
= 13.9

The pH of ammonium phosphate solution, if pK_a of phosphoric acid and pk_b of ammonium hydroxide are
 5.23 and 4.75 respectively, is _____.

Sol. Since $(NH_4)_3PO_4$ is salt of weak acid (H_3PO_4) & weak base (NH_4OH) .

pH 7
$$\frac{1}{2}$$
(pk_a pk_b)
7 $\frac{1}{2}$ (5.23 4.75)

= 7.24 ≈ 7.

PART C : MATHEMATICS

Single Choice Type

This section contains 20 Single choice questions. Each question has 4 choices (1), (2), (3) and (4) for its answer, out of which Only One is correct. 1. If vectors $\vec{a}_1 = x\hat{i} + \hat{j} + \hat{k}$ and $\vec{a}_2 = \hat{i} + y\hat{j} + z\hat{k}$ are collinear, then a possible unit vector parallel to the vector xî yî zk is (1) $\frac{1}{\sqrt{2}}$ \hat{j} \hat{k} (2) $\frac{1}{\sqrt{2}}$ \hat{i} \hat{j} (3) $\frac{1}{\sqrt{3}}$ \hat{i} \hat{j} \hat{k} (4) $\frac{1}{\sqrt{3}}$ \hat{i} \hat{j} \hat{k} Ans. (4) Sol. \vec{a}_1 and \vec{a}_2 are collinear so $\frac{x}{1} = \frac{1}{v} = \frac{1}{z}$ unit vector in direction of $x\hat{i} y\hat{j} z\hat{k} = \frac{1}{\sqrt{3}}\hat{i} \hat{j} \hat{k}$ if k is odd 1 2. Let A = {1, 2, 3, ..., 10} and f : A \rightarrow A be defined as f(k)if k is even Then the number of possible functions $g : A \rightarrow A$ such that gof = f is $(1) 10^{5}$ $(2)^{10}C_{5}$ $(3) 5^{5}$ (4) 5! Ans. (1) x 1, if x is odd x, if x is even Sol. f(x) JEE . \therefore g : A \rightarrow A such that g(f(x)) = f(x) \Rightarrow If x is even then g(x) = x ...(1) If x is odd then g(x + 1) = x + 1 ...(2)from (1) and (2) we can say that g(x) = x if x is even \Rightarrow If x is odd then g(x) can take any value in set A so number of $g(x) = 10^5 \times 1$ Let $f : R \rightarrow R$ be defined as 3. $2\sin \frac{x}{2}$, if x 1 $|ax^2 x b|$, if 1 x 1 f(x) sin x if 1 x 1 If f(x) is continuous on R, then a + b equals: (1) - 3(2) - 1(3) 3 (4) 1

Ans. (2)
Sol.
$$f(x)$$
 is continuous on R
 $\Rightarrow f(1^{-}) = f(1) = f(1^{+})$
 $|a \ 1 \ b| \lim_{x \ 1} x x$
 $|a + 1 + b| = 0 \Rightarrow a + b = -1 ...(1)$
 $\Rightarrow Also f(-1^{-}) = f(-1) = f(-1^{+})$
 $\lim_{y \ 2 \ 2 \ 2 \ 2 \ -1} = 1 \ b| = 2$
Either $a - 1 + b = 2$ or $a - 1 + b = -2$
 $a + b = 3 ...(2) \text{ or } a + b = -1$...(3)
from (1) and (2) $\Rightarrow a + b = -1$
4. For $x > 0$, if $f(x) = \frac{x \ \log_{x} t}{x \ (1 \ t)} dt$, then $f(e) \ f = \frac{1}{e}$ is equal to
(1) 1 (2) -1 (3) $\frac{1}{2}$ (4) 0
Ans. (3)
Sol. $f(x) = \frac{x \ \log_{x} t}{x \ \sqrt{1 \ t}} dt$, let $t = \frac{1}{y}$
 $= \frac{x \ (1 \ t)}{y \ y^{2}} dy$
 $= \frac{x \ (1 \ t)}{y \ y^{2}} dy$
hence
 $f x \ f = \frac{1}{x} = \frac{x \ (1 \ t)}{x \ (1 \ t)} dt$, $\frac{x \ (nt)}{t \ (1 \ t)} dt$
hence
 $f x \ f = \frac{1}{x} = \frac{x \ (1 \ t)}{x \ (1 \ t)} dt$
 $= \frac{1}{e} = \frac{1}{2} \dots (3)$

5. A natural number has prime factorization given by $n = 2^x 3^y 5^z$, where y and z are such that y + z = 5 and $y^1 z^1 \frac{5}{6}$, y > z. Then the number of odd divisors of n, including 1, is : (1) 11 (2) 6 (3) 6x (4) 12

Ans.	(4)
Sol.	y + z = 5
	$\frac{1}{y} \frac{1}{z} \frac{5}{6} \qquad \qquad y > z$
	\Rightarrow y = 3, z = 2
	\Rightarrow n = 2 ^x .3 ³ .5 ² = (2.2.2) (3.3.3) (5.5)
	Number of odd divisors = $4 \times 3 = 12$
6.	Let $f(x) = \sin^{-1}x$ and $g(x) = \frac{x^2 + x + 2}{2x^2 + x + 6}$. If $g(2) = \lim_{x \to 2} g(x)$, then the domain of the function fog is :
	(1) , 2 $\frac{3}{2}$, (2) , 2 1, (3) , 2 $\frac{4}{3}$, (4) , 1 2,
Ans.	(3)
Sol.	Domain of $fog(x) = sin^{-1}(g(x))$
	$ g(x) 1$, $g(2) \frac{3}{7}$
	$\begin{vmatrix} x^{2} & x & 2 \\ 2x^{2} & x & 6 \end{vmatrix} = 1$
	$\begin{vmatrix} x & 1 & x & 2 \\ \hline 2x & 3 & x & 2 \end{vmatrix} 1$
	$\frac{x}{2x} \frac{1}{3} 1 \text{ and } \frac{x}{2x} \frac{1}{3} 1$
	$\frac{x \ 1 \ 2x \ 3}{2x \ 3} \ 0 \text{ and } \frac{x \ 1 \ 2x \ 3}{2x \ 3} \ 0$ $\frac{x \ 2}{2x \ 3} \ 0 \text{ and } \frac{3x \ 4}{2x \ 3} \ 0$
	$\frac{x}{2x} \frac{2}{3} 0 \text{ and } \frac{3x}{2x} \frac{4}{3} 0$
	x , 2 $\frac{4}{3}$,

7.

The triangle of maximum area that can be inscribed in a given circle of radius 'r' is :

(1) An isosceles triangle with base equal to 2r.

(2) An equilateral triangle of height $\frac{2r}{3}$.

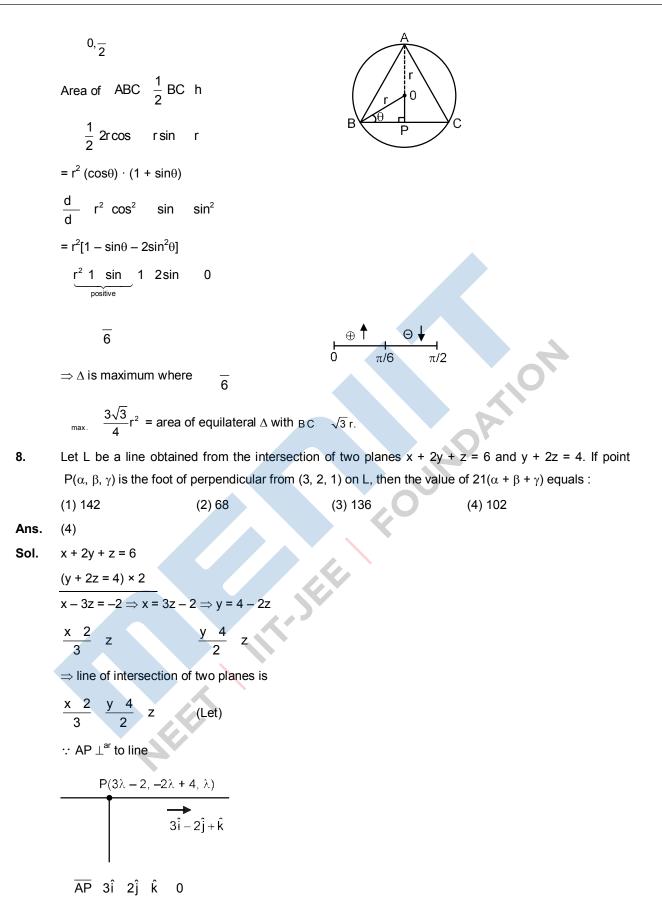
(3) An equilateral triangle having each of its side of length $\sqrt{3}$ r.

(4) A right angle triangle having two of its sides of length 2r and r.

Ans. (3)

Sol. $h = rsin\theta + r$

base = BC = $2rcos\theta$



FOUNDAIL

 $(3\lambda - 5) \cdot 3 + (-2\lambda + 2) (-2) + (\lambda - 1) \cdot 1 = 0$ $9\lambda - 15 + 4\lambda - 4 + \lambda - 1 = 0$ $14\lambda = 20$ $\frac{10}{7} \quad P \quad \frac{16}{7}, \frac{8}{7}, \frac{10}{7}$ $\frac{16}{7} \quad 8 \quad 10}{7} \quad \frac{34}{7}$

 $21(\alpha + \beta + \gamma) = 102$

9.

Let $F_1(A,B,C) = (A \land \neg B) \lor [\neg C \land (A \lor B)] \lor \neg A$ and $F_2(A, B) = (A \lor B) \lor (B \to \neg A)$ be two logical expressions. Then :

- (1) F_1 and F_2 both are tautologies
- (2) F₁ is a tautology but F₂ is not a tautology
- (3) F_1 is not tautology but F_2 is a tautology
- (4) Both F_1 and F_2 are not tautologies

$$\textbf{Sol.} \qquad F_1: (A \wedge \textbf{~B}) \vee [\textbf{~C} \wedge (A \vee B)] \vee \textbf{~A}$$

 $\mathsf{F}_2:(\mathsf{A} \lor \mathsf{B}) \lor (\mathsf{B} \to \mathsf{\sim}\mathsf{A})$

 $\mathsf{F}_1:\{(\mathsf{A}\wedge\mathsf{\sim}\mathsf{B})\vee\mathsf{\sim}\mathsf{A}\}\vee[(\mathsf{A}\vee\mathsf{B})\wedge\mathsf{\sim}\mathsf{C}]$

$$: \{(\mathsf{A} \lor \mathsf{\sim} \mathsf{A}) \land (\mathsf{\sim} \mathsf{A} \lor \mathsf{\sim} \mathsf{B})\} \lor [(\mathsf{A} \lor \mathsf{B}) \land \mathsf{\sim} \mathsf{C}]$$

: {t \land (~A \lor ~B)} \lor [(A \lor B) \land ~C]

 $: (\mathsf{\sim}\mathsf{A} \lor \mathsf{\sim}\mathsf{B}) \lor [(\mathsf{A} \lor \mathsf{B}) \land \mathsf{\sim}\mathsf{C}]$

: <u>~A ~B A B</u> ~A ~B ~C

 F_1 : (~A \lor ~B) \land ~ C \neq t (tautology)

 F_2 : (A \lor B) \lor (~B \lor ~A) = t (tautology)

10. Let slope of the tangent line to a curve at any point P(x, y) be given by $\frac{xy^2 - y}{x}$. If the curve intersects the line x + 2y = 4 at x = -2, then the value of y, for which the point (3, y) lies on the curve, is :

(1)
$$\frac{18}{35}$$
 (2) $\frac{4}{3}$ (3) $\frac{18}{19}$ (4) $\frac{18}{11}$

Ans. (3)

Sol. $\frac{dy}{dx} \frac{xy^2 y}{x}$ $\frac{xdy ydx}{y^2} x dx$ $d \frac{x}{y} \quad x \, dx$ $\frac{x}{y} \frac{x^2}{2} \quad c$

 \therefore curve intersects the line x + 2y = 4 at

x = $-2 \Rightarrow$ point of intersection is (-2, 3)

 \therefore curve passes through (-2, 3)

$$\frac{2}{3} \ 2 \ c \ c \ \frac{4}{3}$$
$$\frac{x}{y} \ \frac{x^2}{2} \ \frac{4}{3}$$

Now put (3, y)

$$\frac{3}{y} \frac{19}{6}$$
$$y \frac{18}{19}$$

11. If the locus of the mid-point of the line segment from the point (3, 2) to a point on the circle, $x^2 + y^2 = 1$ is a circle of radius r, then r is equal to :

(1) 1
(2)
$$\frac{1}{2}$$
(3) $\frac{1}{3}$
(4) $\frac{1}{4}$

Ans. (2)
Sol. h $\frac{\cos 3}{2}$
k $\frac{\sin 2}{2}$
h $\frac{3}{2}^2$ k $1^2 \frac{1}{4}$
(5) $\frac{1}{3}$

12. Consider the following system of equations :

x + 2y – 3z = a

2

2x + 6y - 11z = b

x - 2y + 7z = c,

where a, b and c are real constants. Then the system of equations :

- (1) has a unique solution when 5a = 2b + c
- (2) has infinite number of solutions when 5a = 2b + c
- (3) has no solution for all a, b and c
- (4) has a unique solution for all a, b and c

Ans.	(2)		
Sol.	$P_1 : x + 2y - 3z = a$		
	$P_2: 2x + 6y - 11z = b$		
	$P_3 : x - 2y + 7z = c$		
	Clearly		
	$5P_1 = 2P_2 + P_3$ if $5a = 2b + c$		
	\Rightarrow All the planes sharing a line of intersection		
	\Rightarrow infinite solutions		
13.	If $0 < a, b < 1$, and $\tan^{1} a$ $\tan^{1} b = \frac{1}{4}$, then the	value of	
	(a b) $\frac{a^2 b^2}{2} = \frac{a^3 b^3}{3} = \frac{a^4 b^4}{4} \dots$ is	:	
	(1) $\log_{e} 2$ (2) $e^{2} - 1$	(3) e	(4) $\log_{e} \frac{e}{2}$
Ans.	(1)		0
Sol.	tan ¹a tan ¹b — 0 < a, b < 1		A
	a b 1 ab 1	Ч. (
	a + b = 1 – ab		
	(a + 1)(b + 1) = 2		
	Now $a \frac{a^2}{2} \frac{a^3}{3} \dots b \frac{b^2}{2} \frac{b^3}{3} \dots$		
	$= \log_{e}(1 + a) + \log_{e}(1 + b)$		
	(\because expansion of $\log_{e}(1 + x)$)		
	$= \log_{e}[(1 + a)(1 + b)]$		
	= log _e 2		
14.	The sum of the series $n = \frac{n^2}{(2n-1)!} = \frac{1}{(2n-1)!}$ is equal to	:	
	(1) $\frac{41}{8}e^{-\frac{19}{8}e^{-1}}$ 10 (2) $\frac{41}{8}e^{-\frac{19}{8}e^{-1}}$ 10	(3) $\frac{41}{8}e^{-\frac{19}{8}}e^{-1}$ 10	(4) $\frac{41}{8}e^{-\frac{19}{8}}e^{-1}$ 10
Ans.	(2)		
Sol.	$T_n = \frac{n^2 - 6n - 10}{(2n - 1)!} = \frac{4n^2 - 24n - 40}{4 - (2n - 1)!}$		
	$\frac{(2n \ 1)^2 \ 20n \ 39}{4 \ (2n \ 1)!}$		

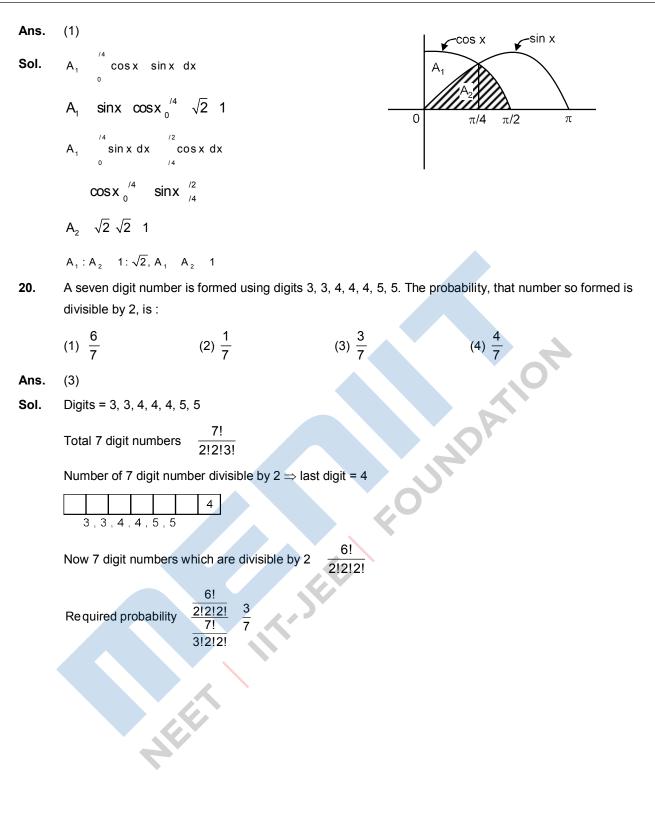
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	$\frac{(2n \ 1)^2}{4} \frac{(2n \ 1)}{(2n \ 1)!}$
	$\frac{1}{4} \frac{(2n \ 1)^2}{(2n \ 1)(2n)!} \frac{(2n \ 1)10}{(2n \ 1)(2n)!} \frac{29}{(2n \ 1)!}$
	$\frac{1}{4} \frac{2n}{(2n)!} \frac{10}{(2n)!} \frac{29}{(2n-1)!}$
	$\frac{1}{4} \frac{1}{(2n-1)!} \frac{11}{(2n)!} \frac{29}{(2n-1)!}$
	$S_1 = \frac{1}{1!} = \frac{1}{3!} = \frac{1}{5!} = \frac{1}{2}$
	$S_2 11 \frac{1}{2!} \frac{1}{4!} \frac{1}{6!} \dots 11 \frac{e}{2} \frac{1}{2}$
	S ₃ 29 $\frac{1}{3!}$ $\frac{1}{5!}$ $\frac{1}{7!}$ 29 $\frac{e}{\frac{1}{2}}$
	Now, S $\frac{1}{4}$ S ₁ S ₂ S ₃
	$\frac{1}{4} \frac{e}{2} \frac{1}{2e} \frac{11e}{2} \frac{11}{2e} \frac{29e}{2} \frac{29}{2e} 4$
	$\frac{41e}{8}$ $\frac{19}{8e}$ 10
15.	Let $f(x)$ be a differentiable function at $x = a$ with $f'(a) = 2$ and $f(a) = 4$. Then $\lim_{x \to a} \frac{xf(a) - af(x)}{x - a}$ equals :
	(1) 2a + 4 (2) 4 - 2a (3) 2a - 4 (4) a + 4
Ans.	(2)
Sol.	f'(a) = 2, f(a) = 4
	$\lim_{x \to a} \frac{xf(a) af(x)}{x a}$
	$\lim_{x \to a} \frac{f(a) - af'(x)}{1}$ (L Hospitals rule)
	= f(a) - af'(a)
	= 4 – 2a
16.	Let A(1, 4) and B(1, -5) be two points. Let P be a point on the circle $(x - 1)^2 + (y - 1)^2 = 1$ such that
	(PA) ² + (PB) ² have maximum value, then the points P, A and B lie on :
	(1) a straight line (2) a hyperbola (3) an ellipse (4) a parabola
Ans.	(1)

P be a point on $(x - 1)^2 + (y - 1)^2 = 1$ Sol. so P(1 + $\cos\theta$, 1 + $\sin\theta$) A(1,4) B(1,-5) $(PA)^{2} + (PB)^{2}$ $= (\cos\theta)^2 + (\sin\theta - 3)^2 + (\cos\theta)^2 + (\sin\theta + 6)^2$ = 47 + 6sinθ is maximum if $\sin\theta = 1$ \Rightarrow sin θ = 1, cos θ = 0 P(1,1) A(1,4) B(1,-5) P,A,B are collinear points. If the mirror image of the point (1, 3, 5) with respect to the plane 4x - 5y + 2z = 8 is (α , β , γ), then 17. $5(\alpha + \beta + \gamma)$ equals : (1) 47 (2) 43(3) 39JUNDATIC Ans. (1) P(1, 3, 5) 4x - 5y + 2z = 8ΜП Sol. Q(θ, β, γ) Point Q is image of point P w.r.to plane, M is mid point of P and Q, lies in plane $M \frac{1}{2}, \frac{3}{2}, \frac{5}{2}$ 4x - 5y + 2z = 8 $4 \frac{1}{2} 5 \frac{3}{2} 2 \frac{5}{2}$ 8 ..(1) Also PQ perpendicular to the plane PQ∥n 5 2 $\frac{1}{4}$ $\frac{3}{5}$ k (let) 1 4k 3 5k ...(2) 5 2k use (2) in (1)

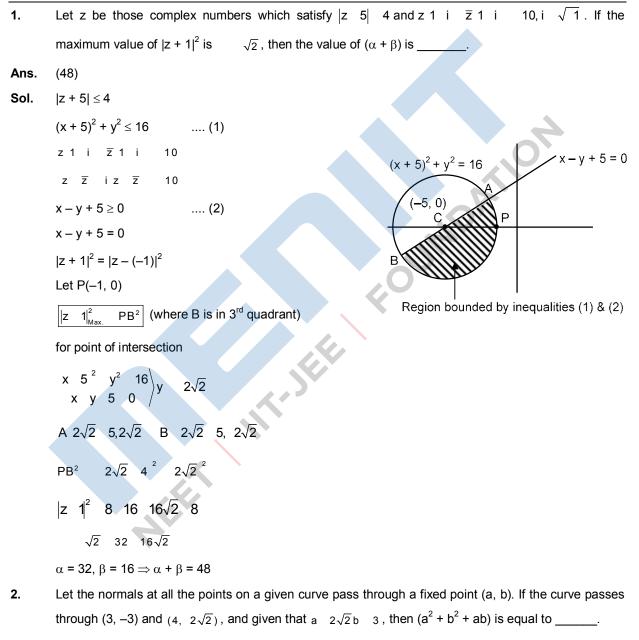
	2 1 4k 5 $\frac{6 5k}{2}$ 10 2k 8
	$k \frac{2}{5}$
	from (2) $\frac{13}{5}$, 1, $\frac{29}{5}$
	$5(\alpha + \beta + \gamma) = 13 + 5 + 29 = 47$
18.	Let $f(x) = e^{t}f(t)dt = e^{x}$ be a differentiable function for all $x \in R$. Then $f(x)$ equals :
	(1) $2e^{e^{x} 1}$ 1 (2) $e^{e^{x}}$ 1 (3) $2e^{e^{x}}$ 1 (4) $e^{e^{x} 1}$
Ans.	(1)
Sol.	$f(x) \int_{0}^{x} e^{t} f(t) dt e^{x} f(0) 1$
	differentiating with respect to x
	$f'(x) = e^{x} f(x) + e^{x}$ $f'(x) = e^{x}(f(x) + 1)$
	$f'(x) = e^{x}(f(x) + 1)$
	$f(x) = e(f(x) + 1)$ $\int_{0}^{x} \frac{f'(x)}{f(x) - 1} dx = \int_{0}^{x} e^{x} dx$ $\ln f(x) - 1 \int_{0}^{x} e^{x} \int_{0}^{x} e^{x} dx$ $\ln (f(x) + 1) - \ln(f(0) + 1) = e^{x} - 1$
	ln f(x) $1 \Big _{0}^{x} e^{x} \Big _{0}^{x}$
	$\ln(f(x) + 1) - \ln(f(0) + 1) = e^{x} - 1$
	$\ln \frac{f(x) \ 1}{2} e^{x} \ 1 \{as \ f(0) = 1\}$
	$f(x) = 2e^{e^x - 1} - 1$

- **19.** Let A_1 be the area of the region bounded by the curves $y = \sin x$, $y = \cos x$ and y-axis in the first quadrant. Also, let A_2 be the area of the region bounded by the curves $y = \sin x$, $y = \cos x$, x-axis and $x = \frac{1}{2}$ in the first quadrant. Then, (1) $A_1 : A_2 = 1 : \sqrt{2}$ and $A_1 = A_2 = 1$ (2) $A_1 = A_2$ and $A_1 = A_2 = \sqrt{2}$ (3) $2A_1 = A_2$ and $A_1 = A_2 = 1 = \sqrt{2}$ (4) $A_1 : A_2 = 1 : 2$ and $A_1 = A_2 = 1$
 - (3) $2A_1 A_2$ and $A_1 A_2 = 1 \sqrt{2}$ (4) $A_1 : A_2 = 1 : 2$ and $A_1 A_2 = 1$



Numeric Value Type

This Section contains 10 Numeric Value Type question, out of 10 only 5 have to be done.



Ans. (9)

Sol. All normals of circle passes through centre

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Radius = CA = CB

$$CA^2 = CB^2$$

 $(a - 3)^2 + (b + 3)^2$
 $(a - 4)^2 + b + 2\sqrt{2}^2$
 $a - 3 - 2\sqrt{2}b - 3$
 $a - 2\sqrt{2}b - 3b - 3 ...(1)$
given that $a - 2\sqrt{2}b - 3 ...(2)$
from (1) & (2) $\rightarrow a = 3, b = 0$
 $a^2 + b^2 + ab = 9$
3. Let α and β be two real numbers such that $\alpha + \beta = 1$ and $\alpha\beta = -1$. Let $p_n = (\alpha)^n + (\beta)^n$, $p_{n-1} = 11$ and
 $p_{n+1} = 29$ for some integer $n \ge 1$. Then, the value of p_n^2 is ______.
Ans. (324)
Sol. $x^2 - x - 1 = 0$ roots = α, β
 $\alpha^2 - \alpha - 1 = 0 \Rightarrow \alpha^{n+1} = \alpha^n + \alpha^{n-1}$
 $\beta^2 - \beta - 1 = 0 \Rightarrow \alpha^{n+1} = \alpha^n + \alpha^{n-1}$
 $\beta^2 - \beta - 1 = 0 \Rightarrow \alpha^{n+1} = \beta^n + \beta^{n-1}$
 $\frac{+}{P_{n-1}} = P_n + P_{n-1}$
 $29 = P_n + 11$
 $P_n = 18$
 $P_n^2 - 324$
4. If $I_{n,n} = \frac{1}{\alpha} x^{n-1} + x^{n-1} dx$ form, $n \ge 1$ and $\frac{4x^n (1 - x^{n-1})}{\alpha - 1 - x^{n-n}} dx$ $I_{n,n}, \alpha \in \mathbb{R}$, then α equals ______.
Ans. (1)
Sol. $I_{n,n} = \frac{1}{\alpha} - \frac{y^{n-1}}{y - 1} - \frac{y^{n-1}}{y - 1} - \frac{y^{n-1}}{y - 1} dy$
so
 $I_{n,n} = \frac{0}{y - 1} - \frac{1}{y - 1} - \frac{y^{n-1}}{y - 1} - \frac{y^{n-1}}{y - 1} - \frac{y^{n-1}}{y - 1} - \frac{y^{n-1}}{y - 1} dy$
so

Now
$$2I_{m,n} = \frac{y^{m-1} - y^{n-1}}{1 - y^{m-n}} dy$$

$$\frac{y^{m-1} - y^{n-1}}{1 - y^{m-n}} dy$$

$$\frac{y^{m-1} - y^{n-1}}{1 - y^{m-n}} dy = \underbrace{\frac{y^{m-1} - y^{n-1}}{1 - y^{m-n}}}_{substitute \ y - \frac{1}{t}} dy$$

$$2I_{m,n} = \frac{1}{0} \frac{y^{m-1} - y^{n-1}}{1 - y^{m-n}} dy = \frac{t^{n-1} - t^{m-1}}{1 - t^{m-n}} \frac{t^{m-n}}{t^{2}} dt$$
Hence $2I_{m,n} = 2\frac{1}{0} \frac{y^{m-1} - y^{n-1}}{1 - y^{m-n}} dy = 1$

If the arithmetic mean and geometric mean of the pth and qth terms of the sequence -16, 8, -4, 2, ... 5. satisfy the equation $4x^2 - 9x + 5 = 0$, then p + q is equal to OUNDATIC

 $4x^2$ 9x 5 0 x 1, $\frac{5}{4}$ Sol.

Now given
$$\frac{5}{4} = \frac{t_p - t_q}{2}$$
, $t = t_q t_q$ where
 $t_r = 16 = \frac{1}{2}^{r-1}$

so
$$\frac{5}{4}$$
 8 $\frac{1}{2}^{p_1}$ $\frac{1}{2}^{q_1}$
1 256 $\frac{1}{2}^{p_{q_2}}$ $2^{p_{q_2}}$

hence p + q = 10

2

The total number of 4-digit numbers whose greatest common divisor with 18 is 3, is _____. 6.

Ans. (1000)

Sol. Let N be the four digit number

gcd(N, 18) = 3

Hence N is an odd integer which is divisible by 3 but not by 9.

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4 digit odd multiples of 3
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1005, 1011,....., 9999 \rightarrow 1500

4 digit odd multiples of 9

1017, 1035,....., 9999 \rightarrow 500

Hence number of such N = 1000

7. Let L be a common tangent line to the curves $4x^2 + 9y^2 = 36$ and $(2x)^2 + (2y)^2 = 31$. Then the square of the slope of the line L is _____.

Sol. Given curves are
$$\frac{x^2}{9} = \frac{y^2}{4}$$

$$x^2 y^2 = \frac{31}{4}$$

let slope of common tangent be m

so tangents are y mx
$$\sqrt{9m^2}$$
 4

y mx
$$\frac{\sqrt{31}}{2}\sqrt{1}$$
 m²

hence $9m^2$ 4 $\frac{31}{4}$ 1 m^2

$$\Rightarrow$$
 36m² +16 = 31+ 31m² \Rightarrow m² = 3

8. Let a be an integer such that all the real roots of the polynomial $2x^5 + 5x^4 + 10x^3 + 10x^2 + 10x + 10$ lie in the interval (a, a + 1). Then, |a| is equal to _____.

Sol. Let $2x^5 + 5x^4 + 10x^3 + 10x^2 + 10x + 10 = f(x)$

Now f(-2) = -34 and f(-1) = 3Hence f(x) has a root in (-2, -1)

Further $f'(x) = 10x^4 + 20x^3 + 20x^2 + 20x + 10$

$$10 x^2 x^2 \frac{1}{x^2} x \frac{1}{x} 20$$

 $10x^2 \times \frac{1}{x} 1^2 17 0$

Hence f(x) has only one real root, so |a| = 2

9. Let $X_1, X_2, ..., X_{18}$ be eighteen observations such that $\prod_{i=1}^{18} x_i$ 36 and $\prod_{i=1}^{18} x_i^2$ 90, where α and

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 β are distinct real numbers. If the standard deviation of these observations is 1, then the value of $|\alpha - \beta|$ is _____.

Sol.
$$\overset{18}{\underset{i 1}{}} x_i \overset{36}{\underset{i 1}{}} \overset{18}{\underset{i 1}{}} x_i \overset{2}{\underset{i 1}{}} 90$$

Hence ${}^{18}x_i^2$ 90 18 2 36 2 Given $\frac{x_i^2}{18} = \frac{x_i}{18}^2 = 1$ \Rightarrow 90 - 18 β^2 + 36 $\beta(\alpha$ + 2) - 18(α + 2)² = 18 \Rightarrow 5 - β^2 + 2 $\alpha\beta$ + 4 β - α^2 - 4 α - 4 = 1 $\Rightarrow (\alpha - \beta)^2 + 4(\alpha - \beta) = 0 \Rightarrow |\alpha - \beta| = 0 \text{ or } 4$ As a and b are distinct $|\alpha - \beta| = 4$ 1 0 0 1 0 0 0 2 0 satisfies the equation A^{20} A^{19} 10. If the matrix A 4 0 for some real 3 0 1 0 0 1 numbers α and β , then $\beta - \alpha$ is equal to _____ OUNDATIC Ans. (4) 1 0 0 0 2 0 Sol. А 3 0 1 1 0 0 1 0 0 1 0 0 A² $0 4 0 A^{3}$ 0 8 0 ,A⁴ 0 16 0 0 0 1 3 0 0 1 0 1 Hence 1 0 0 1 0 0 0 2²⁰ 0 ,A¹⁹ A²⁰ 0 2¹⁹ 0 3 0 0 0 1 1 1 0 0 0 2²⁰ A¹⁹ A So A²⁰ 0 2 0 0 4 0 3 3 1 0 0 0 1 Therefore $\alpha + \beta = 0$ and $2^{20} + 2^{19}\alpha - 2\alpha = 4$ 4 1 2¹⁸ 2 2¹⁸ hence $\beta = 2$ so $(\beta - \alpha) = 4$